

**Program 13 Experimental Study of the Viscoplastic Response of High Temperature Structures** 803

Marshall F. Coyle and E.A. Thornton

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**Objectives**

The basic objective of this research program is to investigate experimentally the viscoplastic response of thermal structures for high speed flight. An additional objective of the experimental program is to provide high quality data for validation of finite element analysis using unified viscoplastic constitutive models.

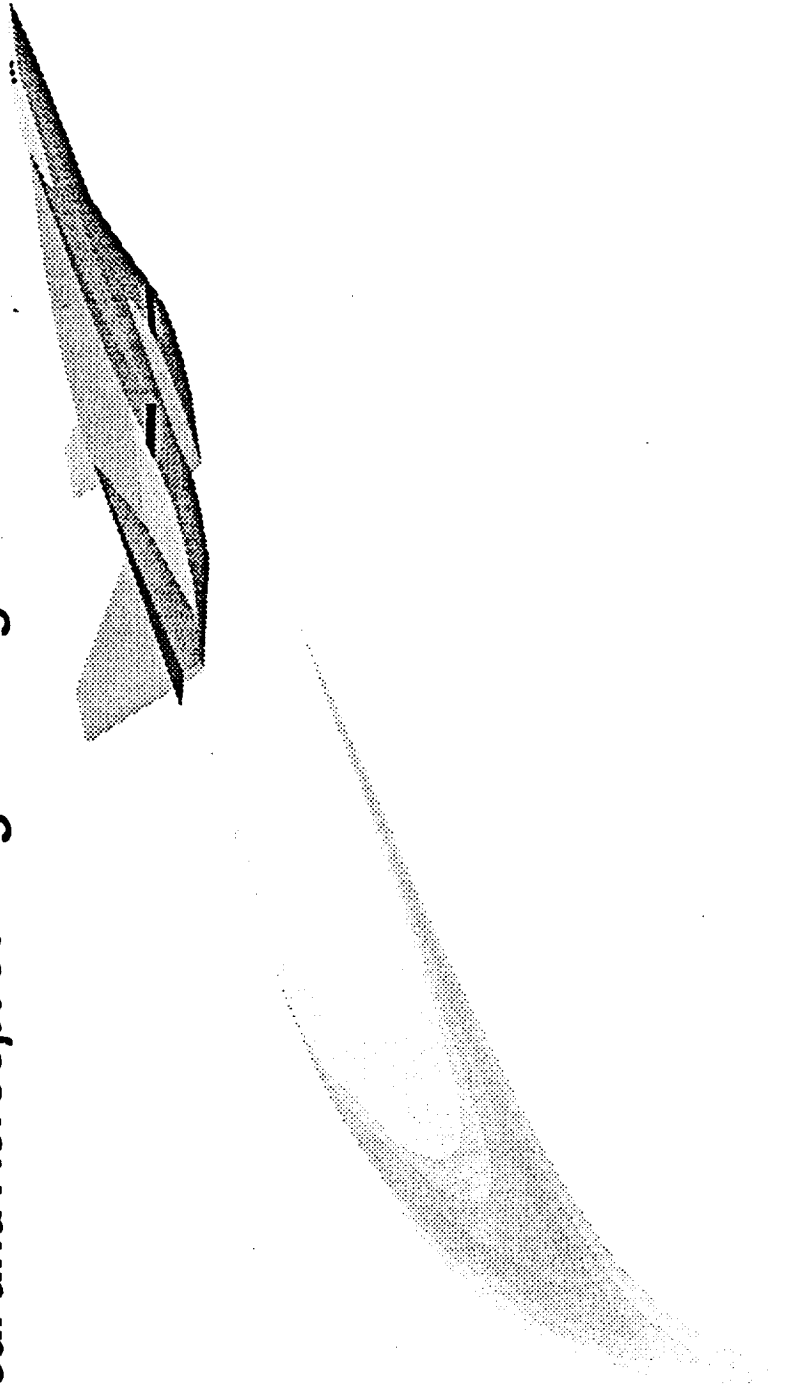
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# EXPERIMENTAL AND COMPUTATIONAL STUDIES OF THERMOVISCOPLASTIC PANELS

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***Earl A. Thornton***  
***Marshall Coyle***

***Mechanical and Aerospace Engineering***



EXPERIMENTAL AND COMPUTATIONAL STUDIES  
OF THERMOVISCOPLASTIC PANELS

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Marshall F. Coyle, Graduate Student

Department of Mechanical and Aerospace Engineering

Abstract

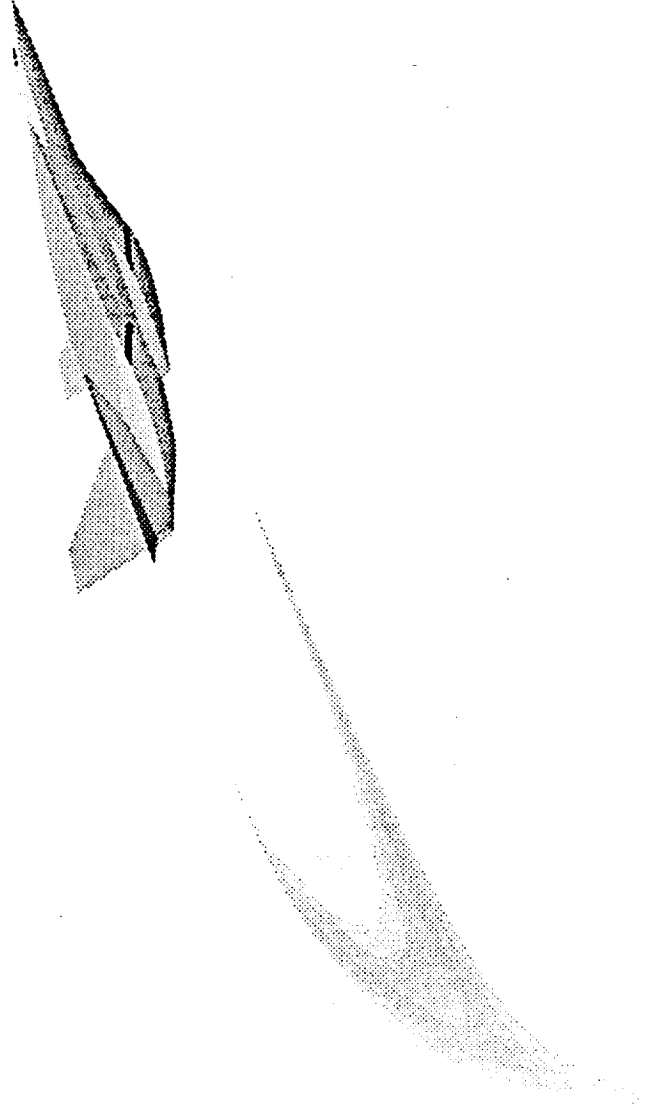
The presentation describes computational and experimental studies of the thermal-structural behavior of thin panels subjected to localized heating. Three research tasks are described: (1) development of a finite element thermoviscoplastic computational approach, (2) experimental determination of material parameters for Bodner-Partom constitutive models of panel materials, and (3) experimental study of "Heldenfels" panels subjected to intense local heating. Recent research progress in each task is reviewed. Development of a new experimental set-up for the panel tests is described in detail and preliminary test results are presented. Plans for future research are highlighted.

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## **RESEARCH OBJECTIVES**

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- Investigate Thermoviscoplastic (TVP) response of thin panels subject to intense local heating.
- Evaluate finite element Thermal-Structural analyses with unified TVP constitutive models by comparison with experimental data.



**THERMOVISCOPLASTIC RESEARCH PROGRAM**

● **FINITE ELEMENT TVP ANALYSIS**

**J. D. KOLENSKI**

● **BODNER-PARTOM CONSTITUTIVE MODELS**

**MARK A. ROWLEY**

● **THERMAL-STRUCTURAL TESTS OF PANELS**

**MARSHALL F. COYLE**

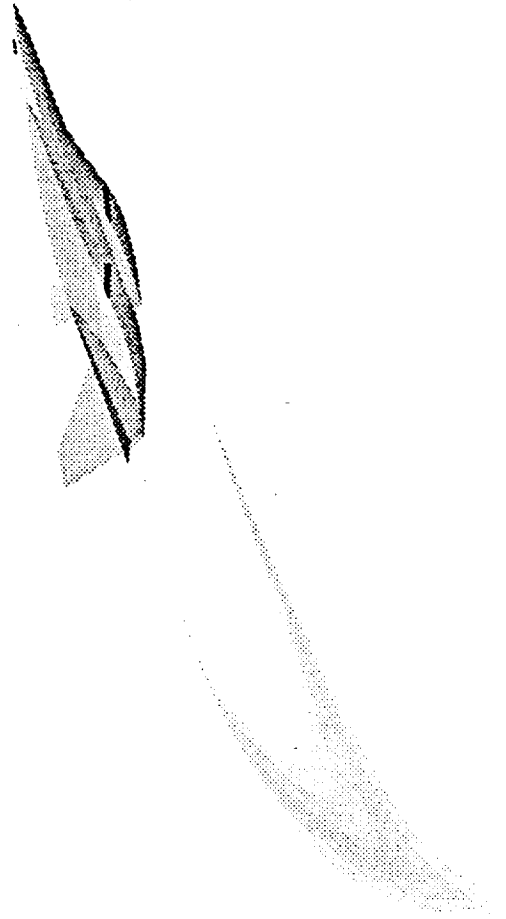
# **FINITE ELEMENT THERMOVISCOPLASTIC ANALYSIS**

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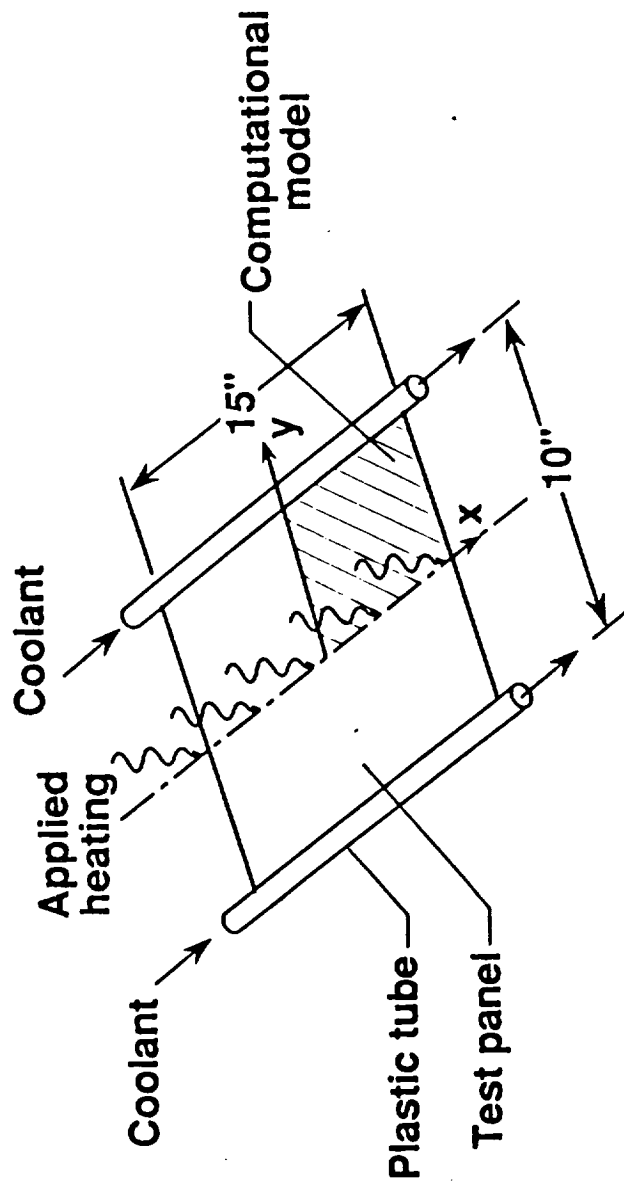
## ***FINITE ELEMENT THERMOVISCOPLASTIC ANALYSIS***

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- ASSUMES QUASI-STATIC THERMAL STRESS BEHAVIOR
  - Neglects Thermal-Mechanical Coupling in Energy Equation
  - Neglects Inertia Forces in Equations of Motion
- ASSUMES PLANE STRESS
- USES BODNER-PARTOM CONSTITUTIVE MODEL
- IMPLEMENTS EQUATIONS IN RATE FORM AND USES TIME-MARCHING ALGORITHM



# HASTELLOY-X PANEL



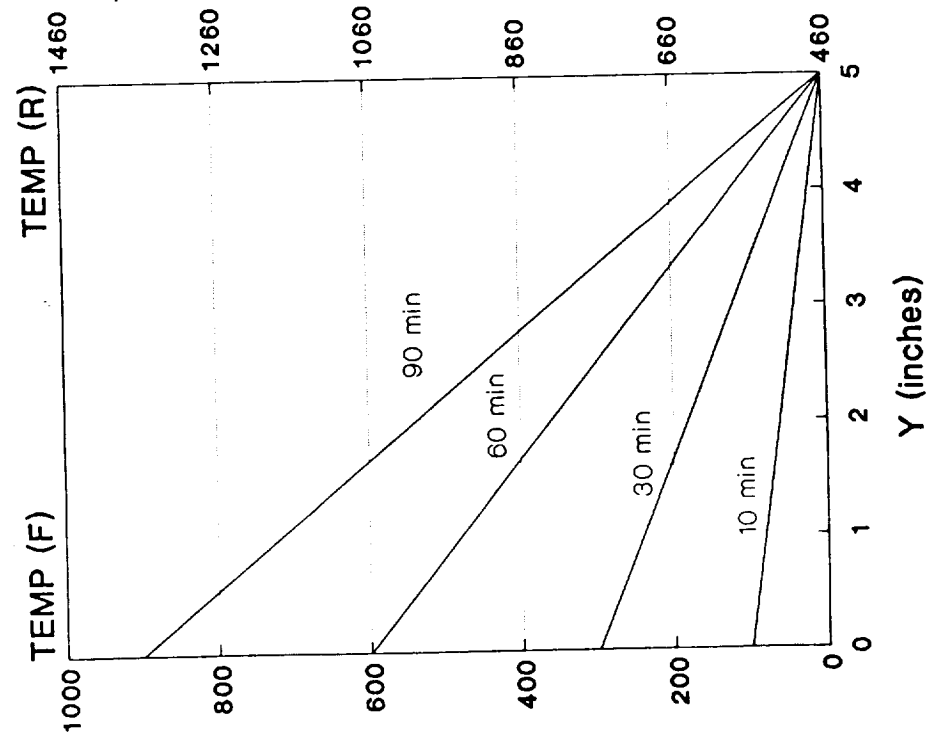
## Finite Element Meshes:

	Slowly Heated	Rapidly Heated
Nodes:	176	187
	uniform	stretched
Elements:	150	320
	quads	triangles

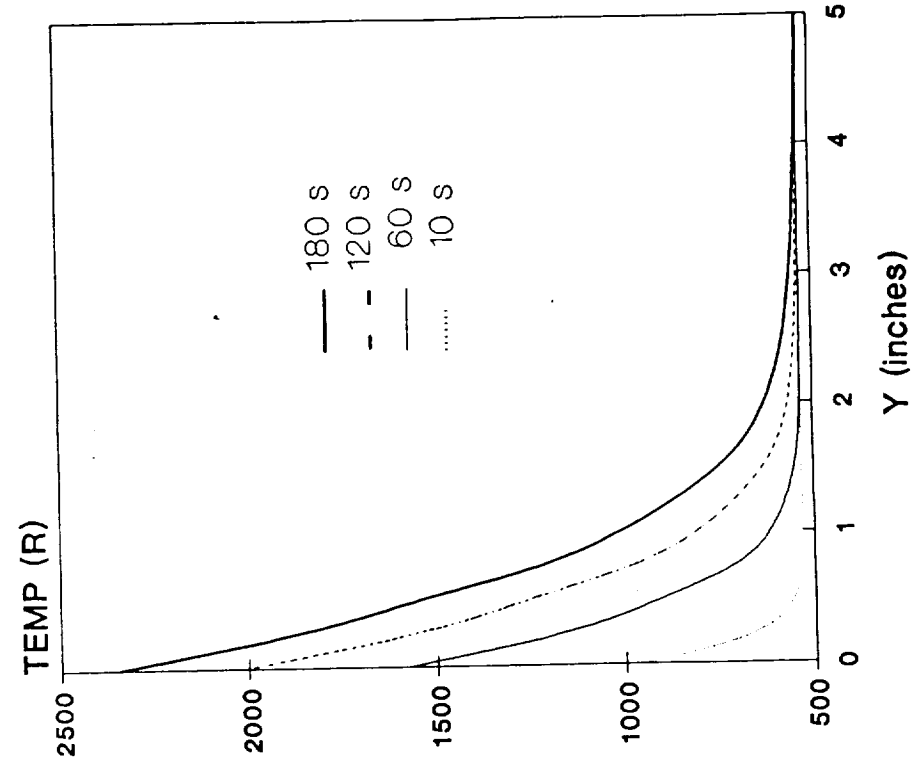


# HASTELLOY-X PANEL TEMPERATURES

## SLOWLY HEATED

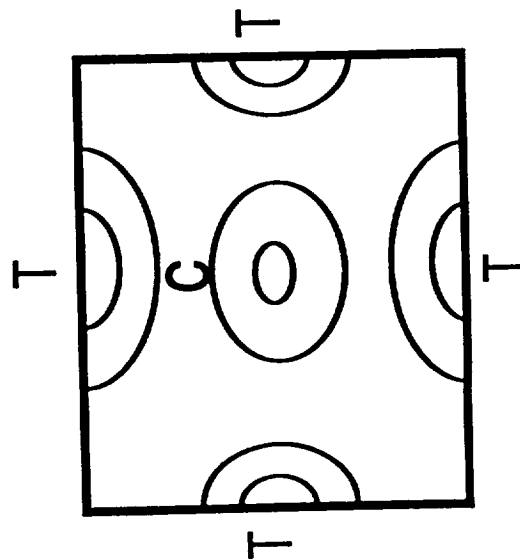


## RAPIDLY HEATED

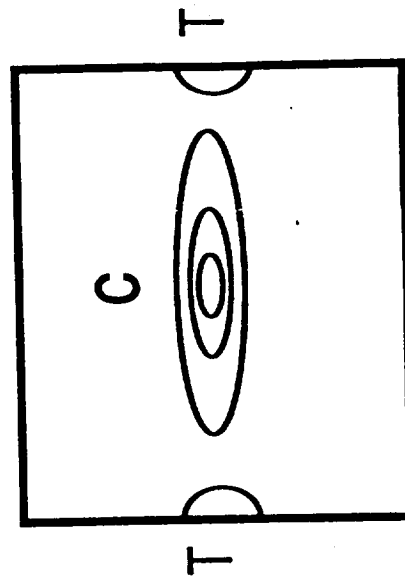


# YIELDED REGIONS

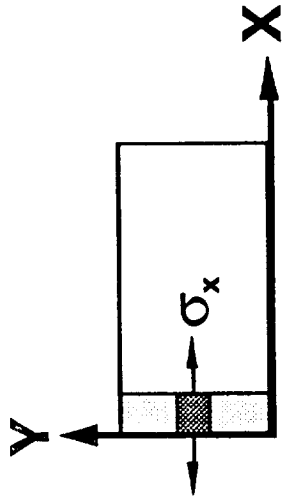
SLOWLY HEATED



RAPIDLY HEATED

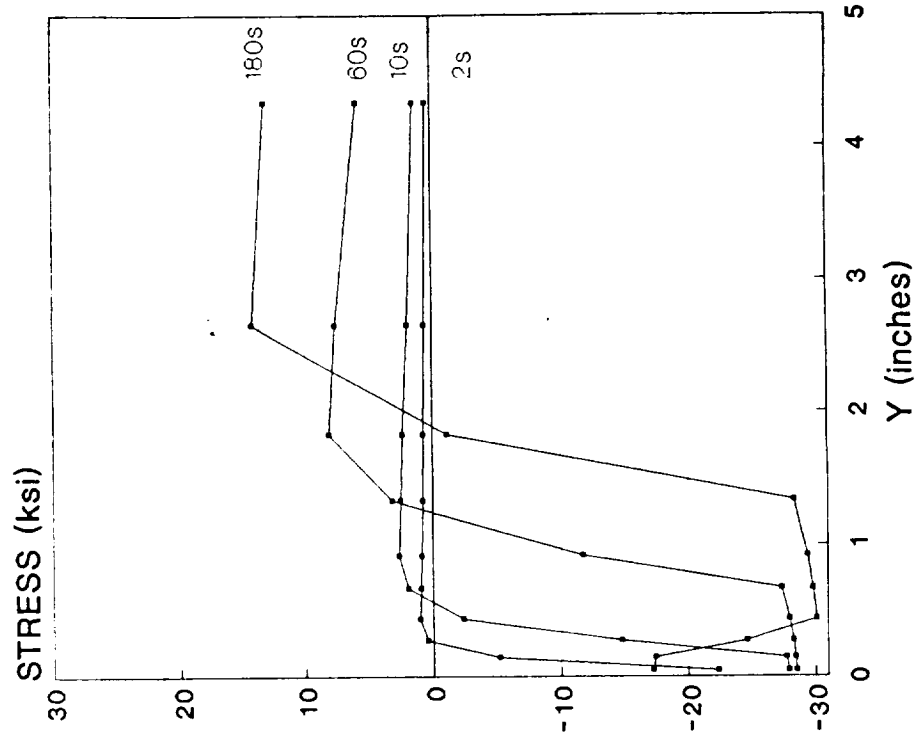
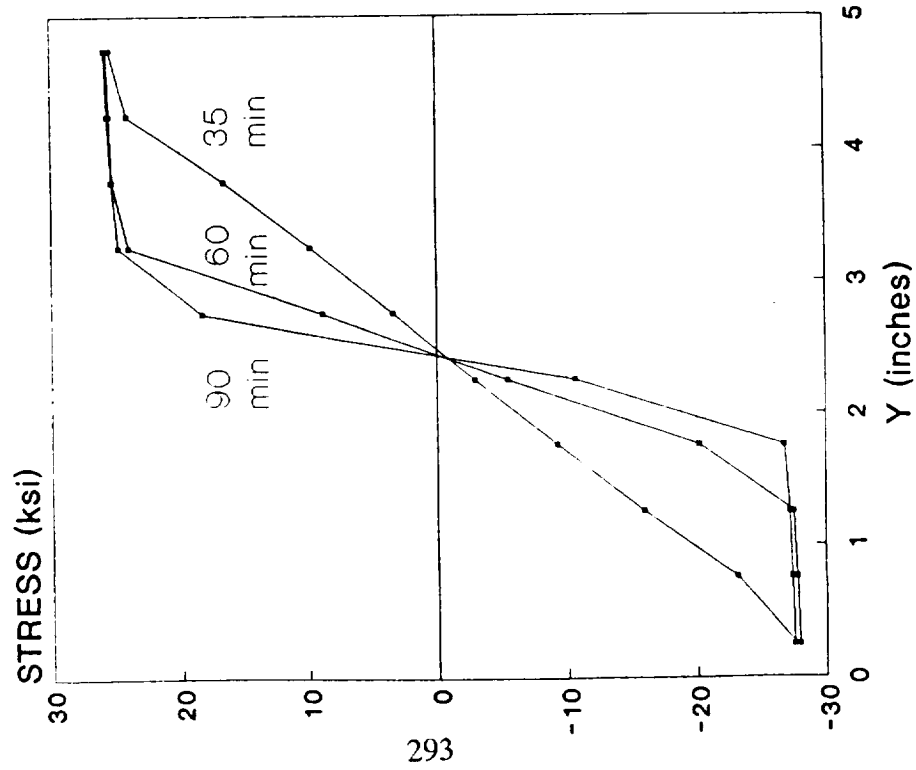


# RECTANGULAR PANEL INELASTIC STRESSES



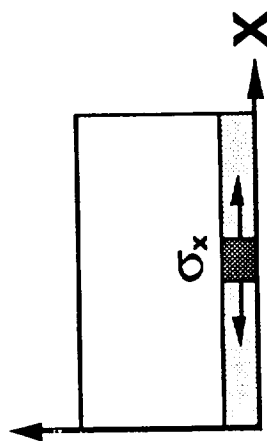
Slowly  
Heated

Rapidly  
Heated



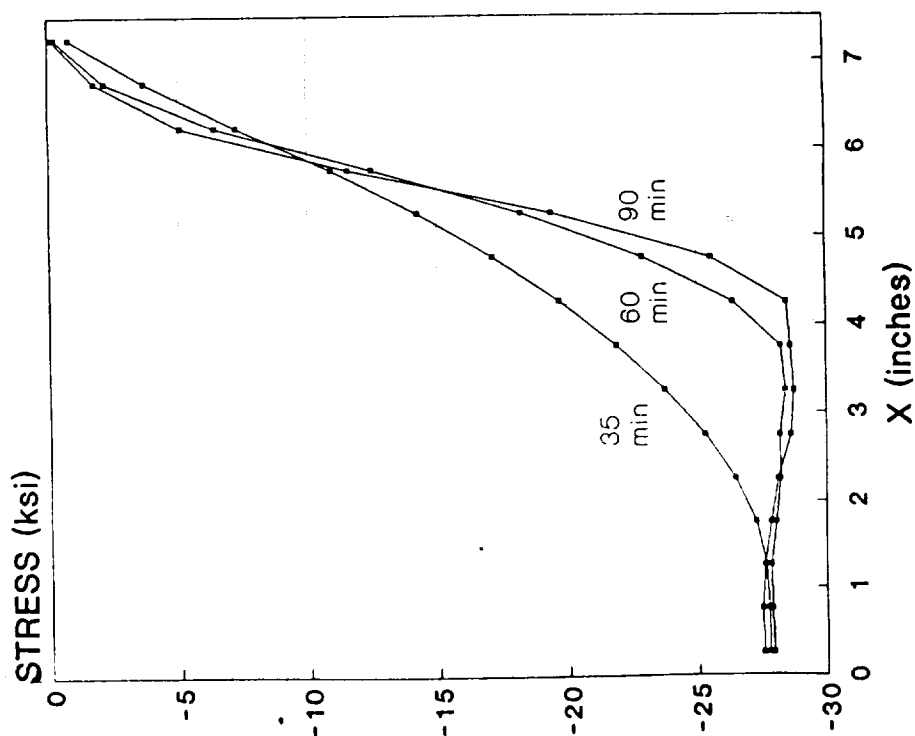
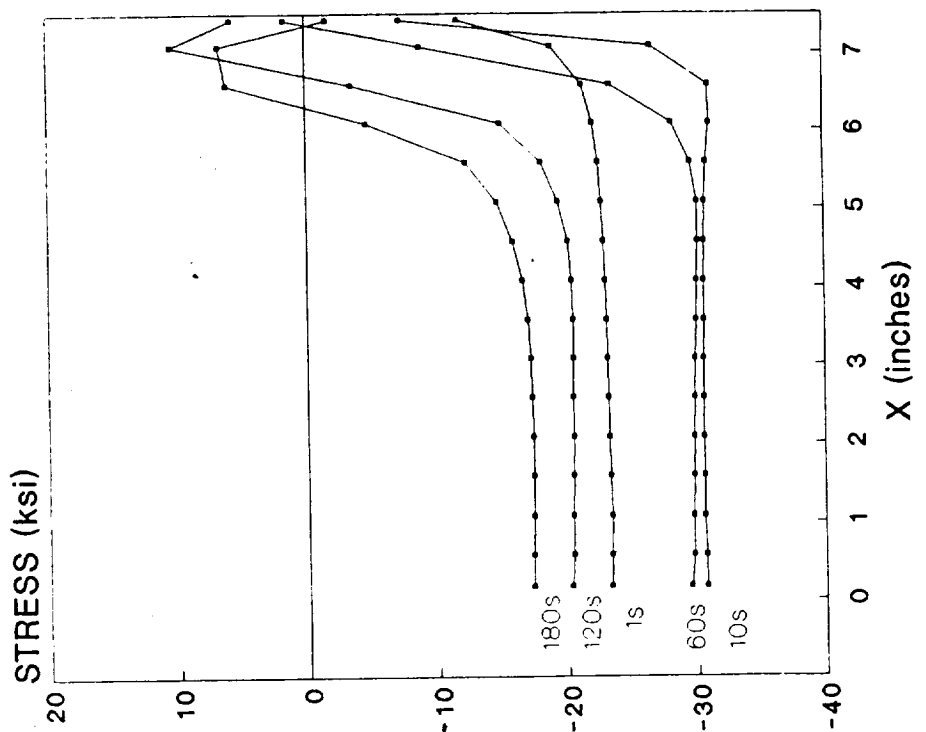
# RECTANGULAR PANEL INELASTIC STRESSES

Y

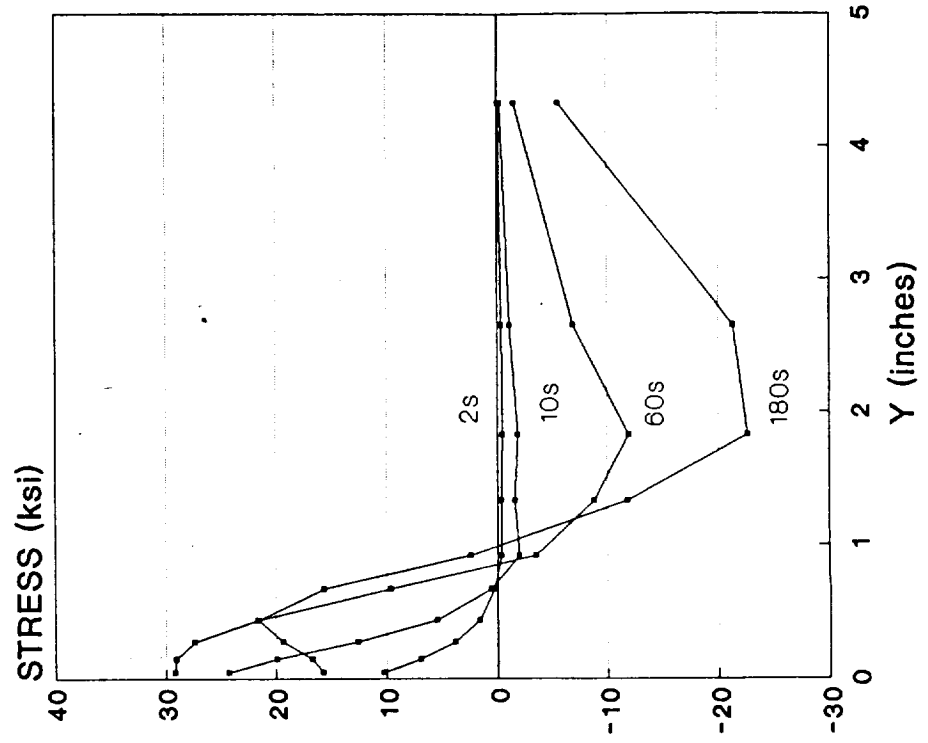
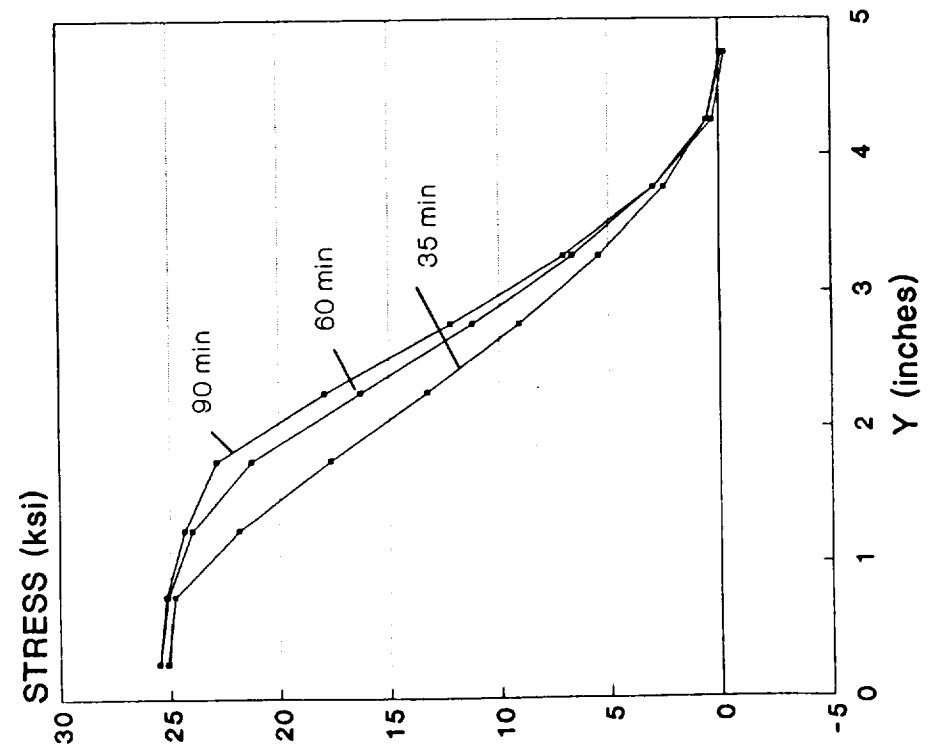
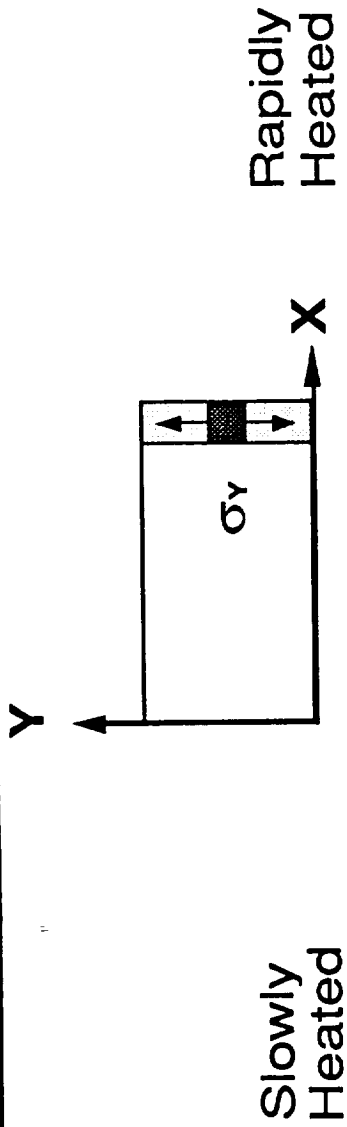


Rapidly  
Heated

Slowly  
Heated



# RECTANGULAR PANEL INELASTIC STRESSES



## **CONCLUSIONS FROM PLANE STRESS COMPUTATIONS**

- **TEMPERATURE RISE TIMES AND LEVELS SIGNIFICANT**
- **FOR RAPID TEMPERATURE RISES:**
  - HIGHER YIELD STRESSES FROM STRAIN-RATE EFFECTS
- **AT ELEVATED TEMPERATURES:**
  - MATERIAL YIELD STRENGTH AND STIFFNESS DEGRADE RAPIDLY
  - PRONOUNCED PLASTIC DEFORMATION

## **EXTENSION OF COMPUTATIONS TO PLATE BENDING**

- **FINITE ELEMENT PLATE BENDING  
WITH VON KARMAN PLATE THEORY**
- **REPRESENT INITIAL PANEL DEFORMATIONS AND THERMAL BUCKLING**
- **BODNER-PARTOM CONSTITUTIVE MODEL**
- **QUASI-STATIC RESPONSE**
- **THERMAL AND MECHANICAL LOADS**
- **TVP RATE FORMULATION**

## FINITE ELEMENT FORMULATION

$$[K_m + K_b + K_g(N)]\{\dot{\delta}\} + [K_g(N)]\{\dot{\delta}\} = \{\dot{F}_p\} + \{\dot{F}_T\} + \{\dot{F}_\sigma\}$$

where:

$[K_m]$  = Membrane Stiffness Matrix

$[K_b]$  = Bending Stiffness Matrix

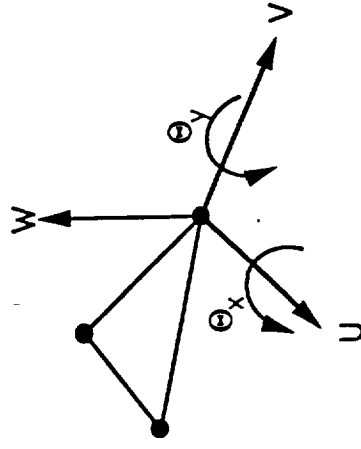
$[K_g(N)]$  = Geometric Stiffness Matrix

$N$  = Membrane Forces

$\{\dot{F}_p\}$  = Plastic Strain

$\{\dot{F}_T\}$  = Temperature

$\{\dot{F}_\sigma\}$  = Surface Traction



DKT Plate Bending Element



## **FINITE ELEMENT APPLICATIONS**

### **VALIDATION STUDIES:**

#### **1. CLASSICAL ELASTIC PLATES (COMPLETED)**

#### **2. ELASTIC VON KARMAN PLATES**

**-LEVY AND CLOUGH FOR PRESSURE LOADS (CURRENT)**

**-GOSSARD, ET AL. FOR HELDENFELS PLATE (PLANNED)**

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### **ELASTIC AND INELASTIC STUDIES (PLANNED):**

#### **3. SLOWLY HEATED HASTELLOY PANELS**

#### **4. RAPIDLY HEATED HASTELLOY PANELS**

#### **5. ALUMINUM ALLOY PANELS**

## **BODNER-PARTOM CONSTITUTIVE MODELS**

# **APPROACH FOR CONSTITUTIVE MODEL DEVELOPMENT**

- 1. Review Bodner-Partom Model**
- 2. Study SwRI Experimental Procedure**
- 3. Simulate Material Constant Determination  
Procedure for B1900+Hf**
- 4. Begin Experimental Program for**
  - Hastelloy-X**
  - 8009 Aluminum Alloy**
- 5. Validate Bodner-Partom Model**

# ESSENTIAL EQUATIONS FOR THE UNI-DIRECTIONAL BODNER-PARTOM CONSTITUTIVE MODEL

1.  $\dot{\varepsilon}_t = \dot{\varepsilon}_e + \dot{\varepsilon}_p$
2.  $\dot{\varepsilon}_p = (2/\sqrt{3})D_0\{\sigma/|\sigma|\}\exp\{-.5(Z/\sigma)^{2n}\}$
3.  $Z = Z^I + Z^D$
4.  $\dot{Z}^I = m_1(Z_1 - Z^I)\dot{W}_p - A_1 Z_1 \{ (Z^I - Z_2)/Z_1 \}^{r_1}$
5.  $\dot{Z}^D = m_2(Z_3 - Z^D)\dot{W}_p - A_2 Z_1 \{ Z^D/Z_1 \}^{r_2}$
6.  $\dot{W}_p = \sigma(\dot{\varepsilon}_p)$

# MATERIAL CONSTANTS IN THE BODNER-PARTOM CONSTITUTIVE MODEL

TEMP. INDEPENDENT	TEMP. DEPENDENT
$D_0$ : Limiting shear strain rate [sec <sup>-1</sup> ]	$Z_0$ : Initial value of isotropic hardening variable [psi]
$Z_1$ : Limiting (maximum) value of $Z^I$ [psi]	$Z_2$ : Fully recovered (minimum) value of $Z^I$ [psi]
$Z_3$ : Limiting (maximum) value of $Z^D$ [psi]	$n$ : Kinetic parameter
$m_1$ : Hardening rate coeff. of $Z^I$ [psi <sup>-1</sup> ]	$A_1$ : Recovery coeff. for $Z^I$ [psi]
$m_2$ : Hardening rate coeff. of $Z^I$ [psi <sup>-1</sup> ]	$A_2$ : Recovery coeff. for $Z^D$ [psi]
	$r_1$ : Recovery exponent for $Z^I$
	$r_2$ : Recovery exponent for $Z^D$

## **PROCEDURE FOR OBTAINING BODNER-PARTOM CONSTANTS (SWRI)**

1. Conduct a series of Multi-Strain-Rate Uniaxial Tensile Tests

2. Obtain a Polynomial that approximates  $\sigma$  vs.  $\epsilon_p$

3. Using the polynomial data, generate a plot of  $\gamma$  vs.  $\sigma$

$$\text{where } \gamma = (1/\sigma)(d\sigma/d\epsilon_p)$$

4. Obtain  $m_1$  and  $m_2$  from the slopes of  $\gamma$  vs.  $\sigma$

5. Set  $D_0$  (usually taken to be  $1 \times 10^4 \text{ sec}^{-1}$ )

6. Obtain  $n$  from saturation stress ( $\sigma_s$ ) vs. strain rate

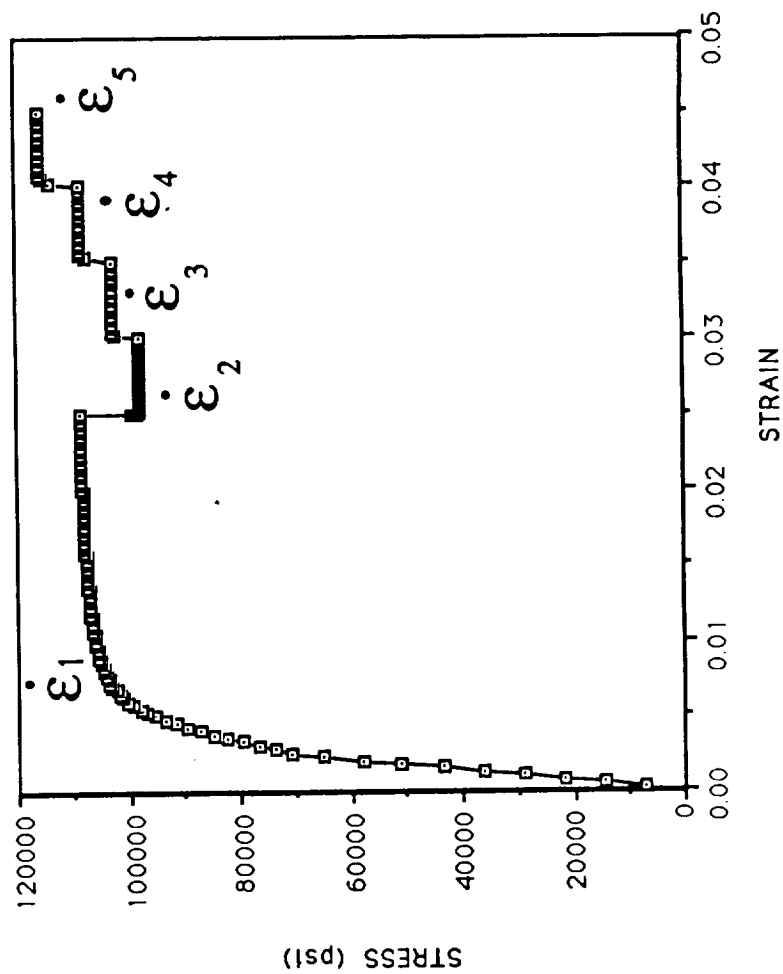
7. Calculate sum of  $Z_1$  and  $Z_3$  from  $\sigma_s$ ,  $n$ , and  $\dot{\epsilon}_p$

8. Obtain  $Z_0$  from 0.2% offset yield stress; Set  $Z_2 = Z_0$

9. Calculate  $Z_1$  from  $\sigma_{\text{yield}}$  and  $\sigma_s$ ; Obtain  $Z_3$

10. Calculate  $A_1 (=A_2)$  and  $r_1 (=r_2)$  from slow rate ( $\epsilon_2$ ) tensile data

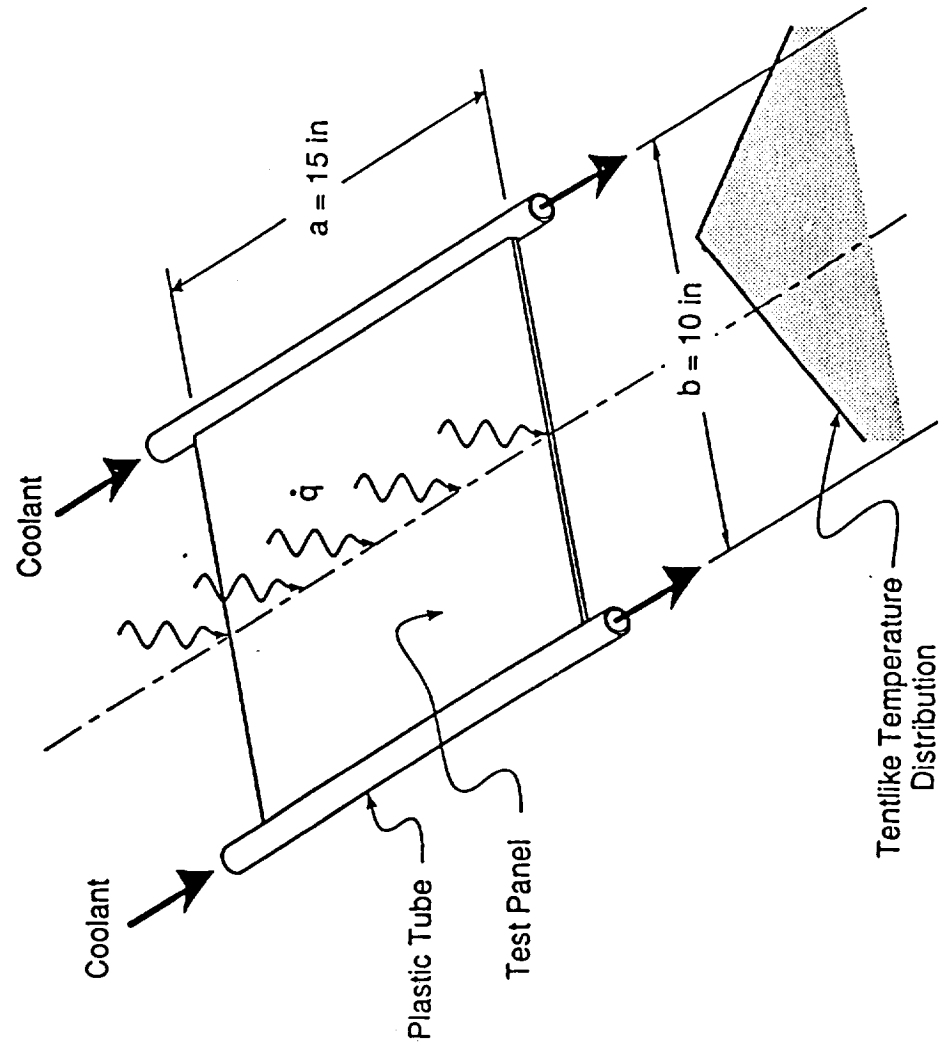
# SIMULATED TENSION TEST WITH STRAIN RATE JUMPS



## **THERMAL-STRUCTURAL TESTS OF PANELS**



## HELDENFELS PROBLEM



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## EXPERIMENTAL PROGRESS

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### PHASE 1 - INSTRUMENTATION OF HASTELLOY PANELS

- *Measured Hastelloy-X Panels' Initial Deformations*
- *Installed PC Based Data Acquisition System*
- *Installed Strain Gages and Thermocouples*
- *Installed LVDTs To Measure Out of Plane Displacement*

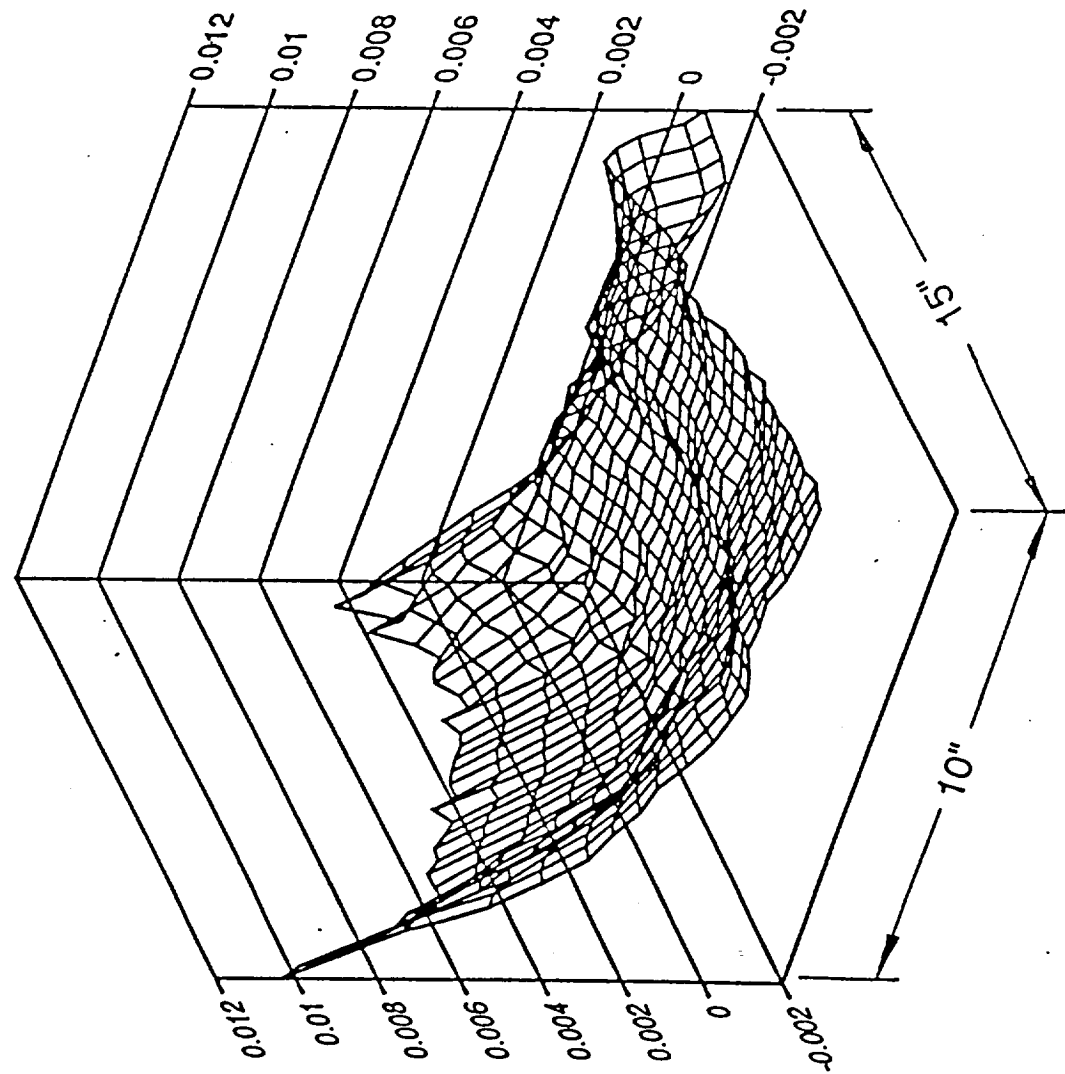
### PHASE 2 - DESIGN AND FABRICATE TEST FIXTURE

- *Incorporated Line Heater*
- *Installed and Tested Coolant Tubes and Chill Water System*
- *Provided Four Point Supports For Test Panel*
- *Provided Mounts for LVDTs*

### PHASE 3 - BEGAN TESTING HASTELLOY-X PANELS

- *Using Line Heater*
- *Evaluated Temperature Distribution*
- *Evaluated LVDTs Data*

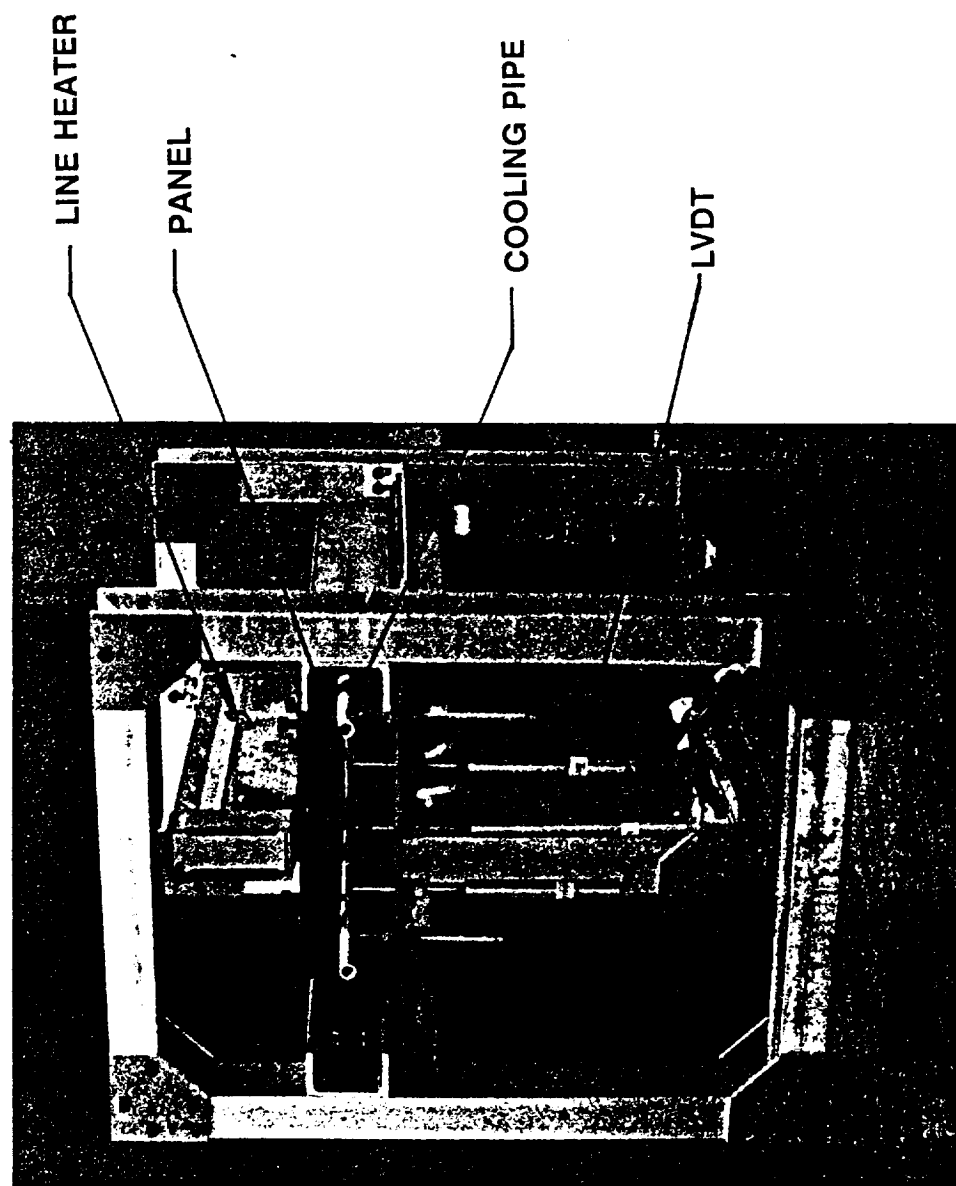
**HASTELLOY-X PANEL**  
**MEASURED INITIAL DISPLACEMENTS**



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## TEST FIXTURE FOR THERMAL-STRUCTURAL TESTS OF PANELS

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OF POOR QUALITY

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**INITIAL TEST RESULTS**

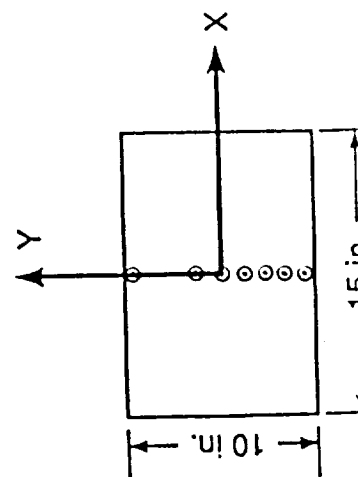
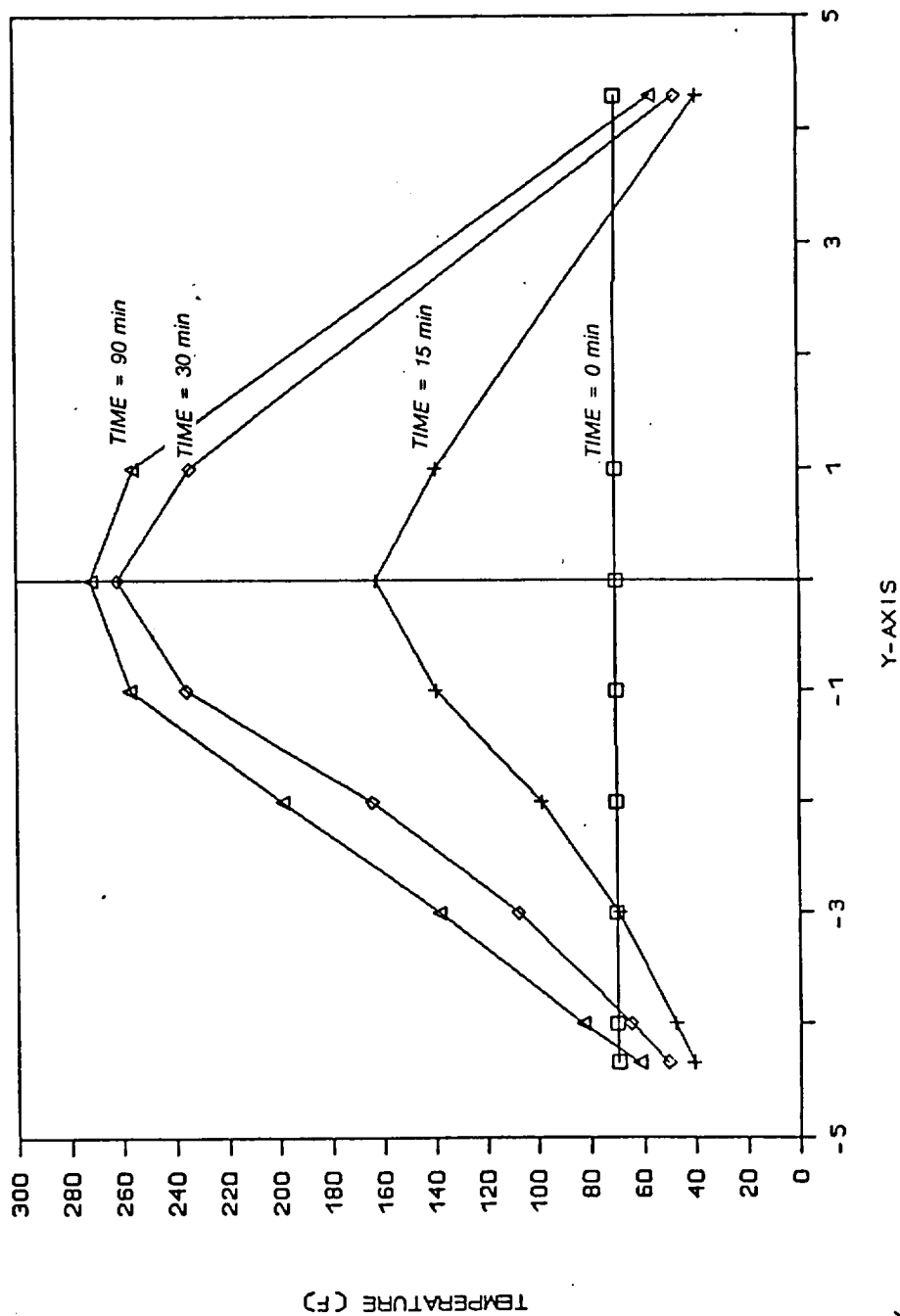
**FOR SLOWLY HEATED HASTELLOY-X PANEL**

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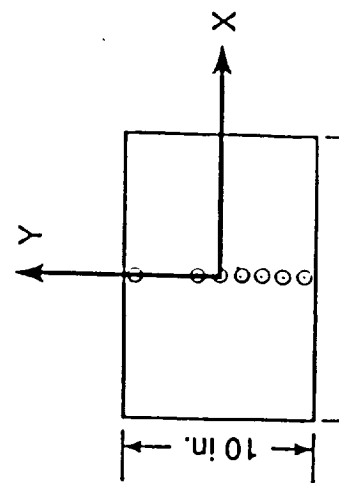
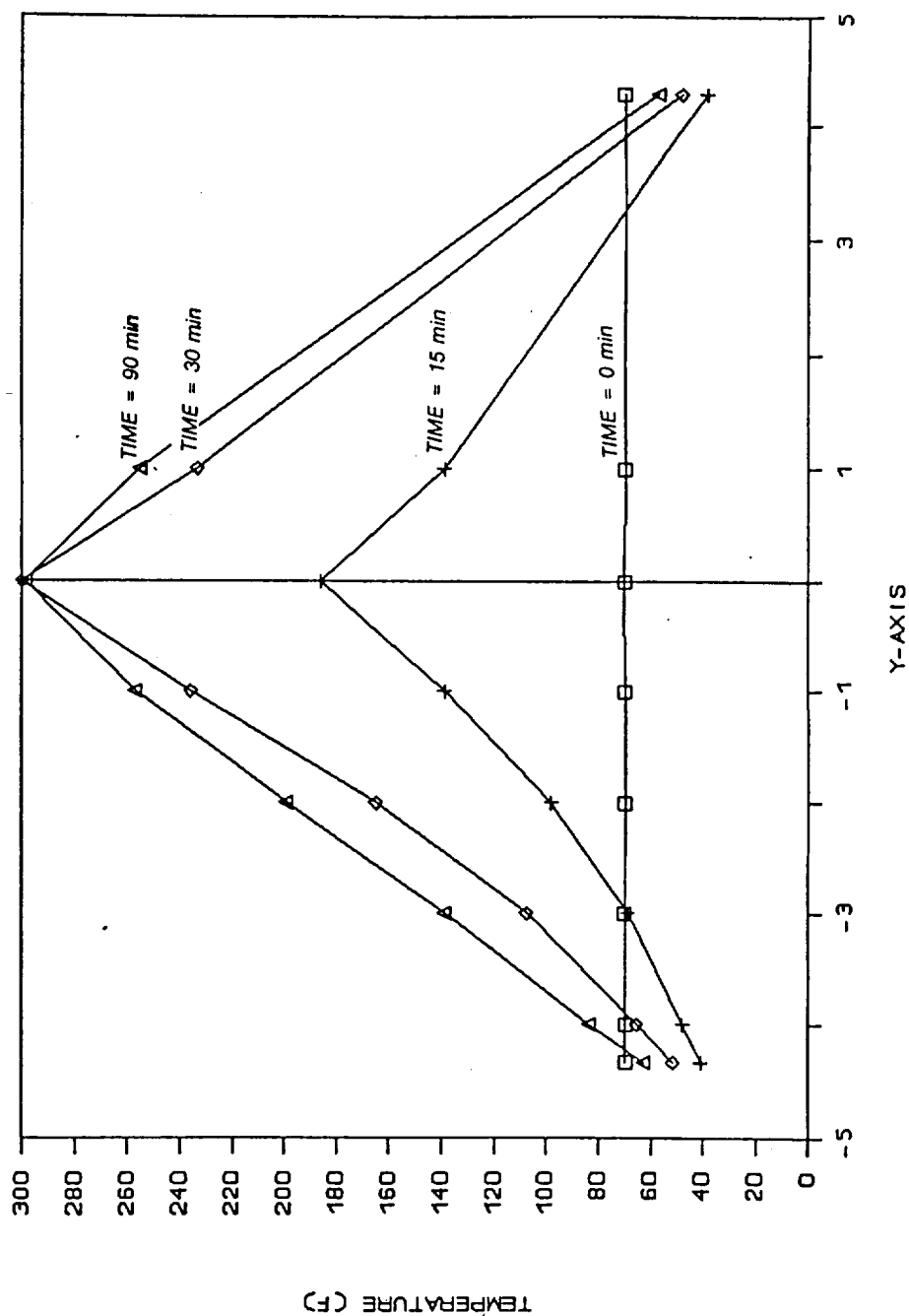
- **TEMPERATURE DISTRIBUTIONS**
- **TEMPERATURE HISTORIES**
- **DISPLACEMENT HISTORIES**

# EXPERIMENTAL TEMPERATURES FOR TEST PANEL

## TEMPERATURE PROFILE ALONG Y AXIS

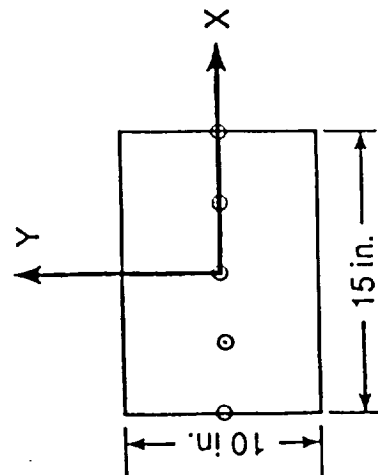
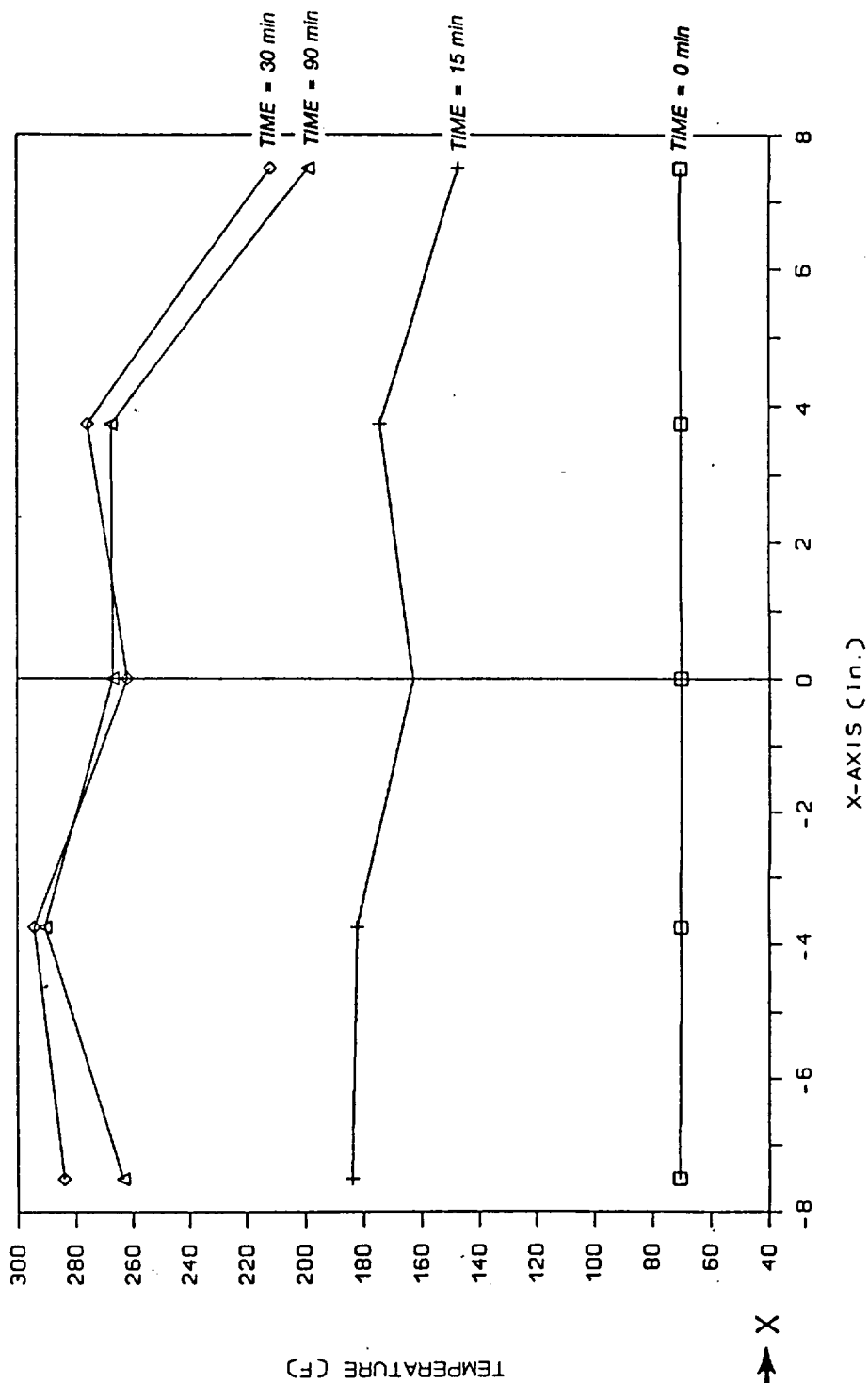


# EXPERIMENTAL TEMPERATURES FOR TEST PANEL TEMPERATURE PROFILE ALONG Y AXIS (WITHOUT LVDT)



# EXPERIMENTAL TEMPERATURES FOR TEST PANEL

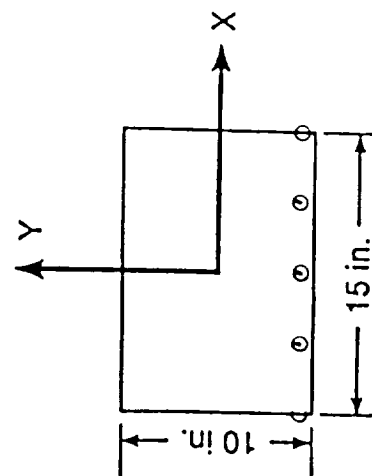
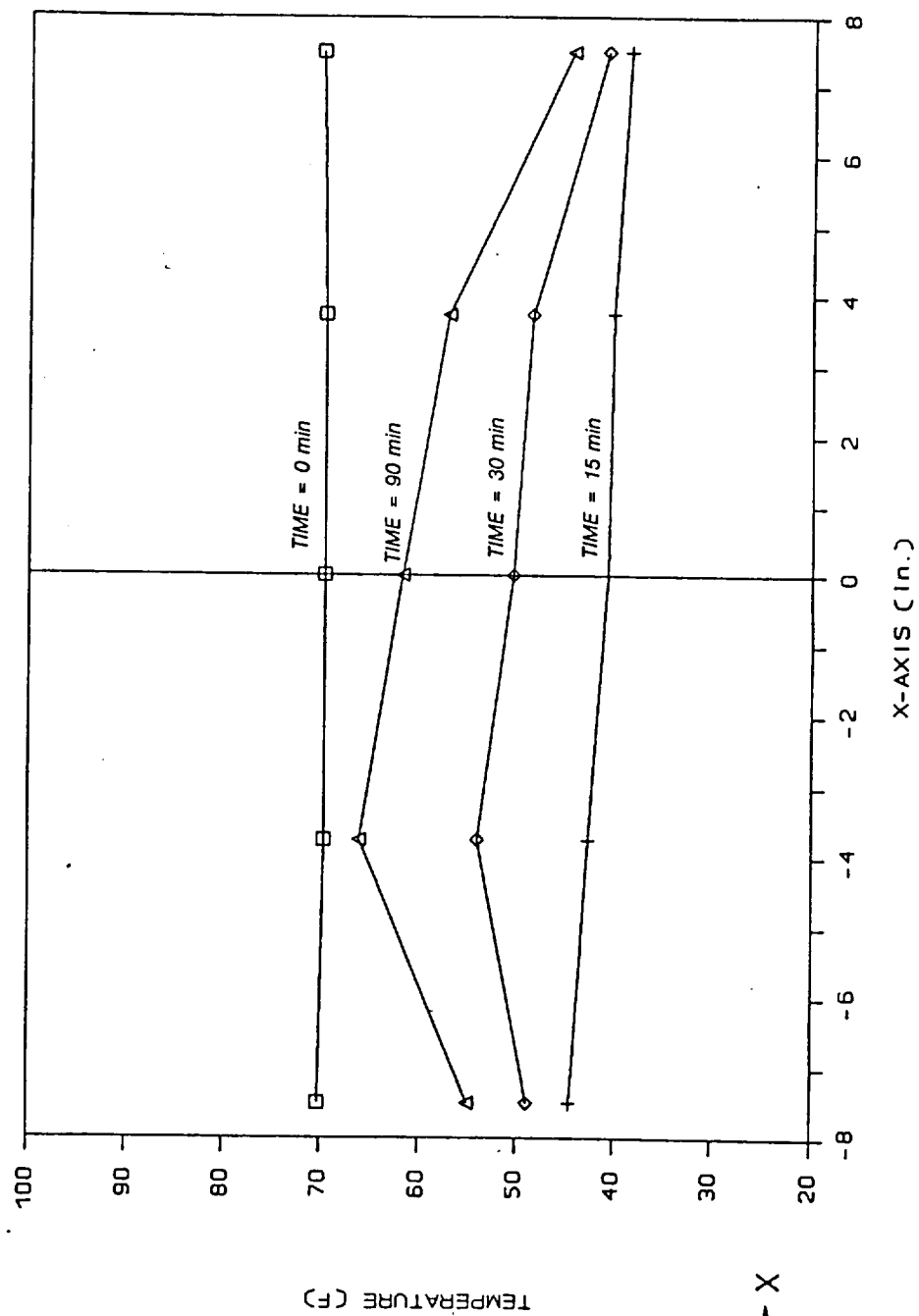
## TEMPERATURES TAKEN ALONG X AXIS



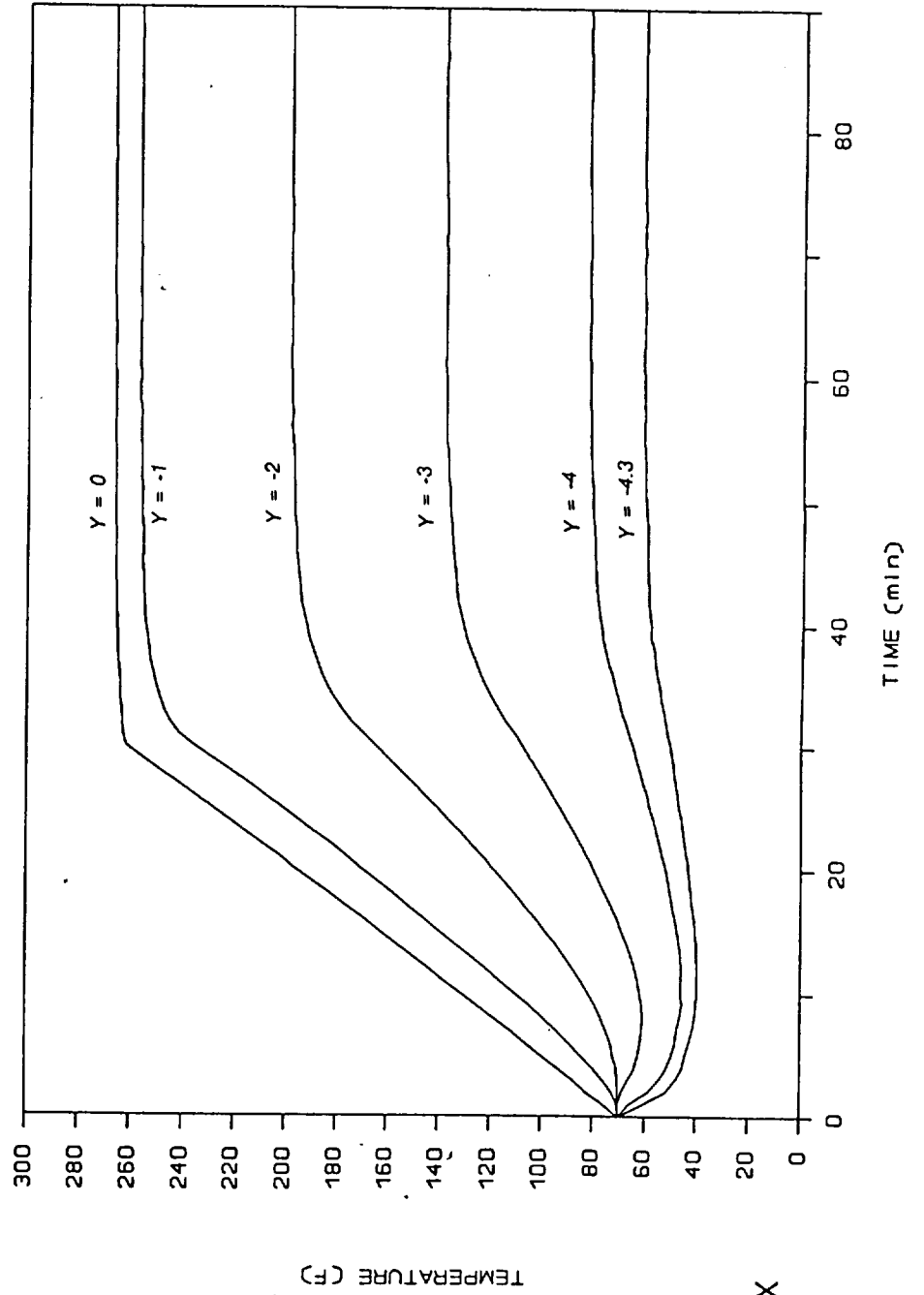


# EXPERIMENTAL TEMPERATURES FOR TEST PANEL

TEMPERATURES TAKEN NEAR THE COOLED EDGE ( $\gamma = -4.3$ )

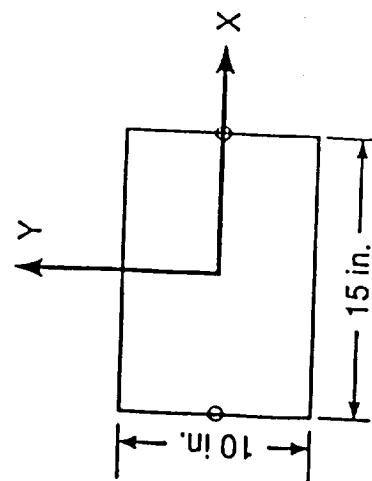
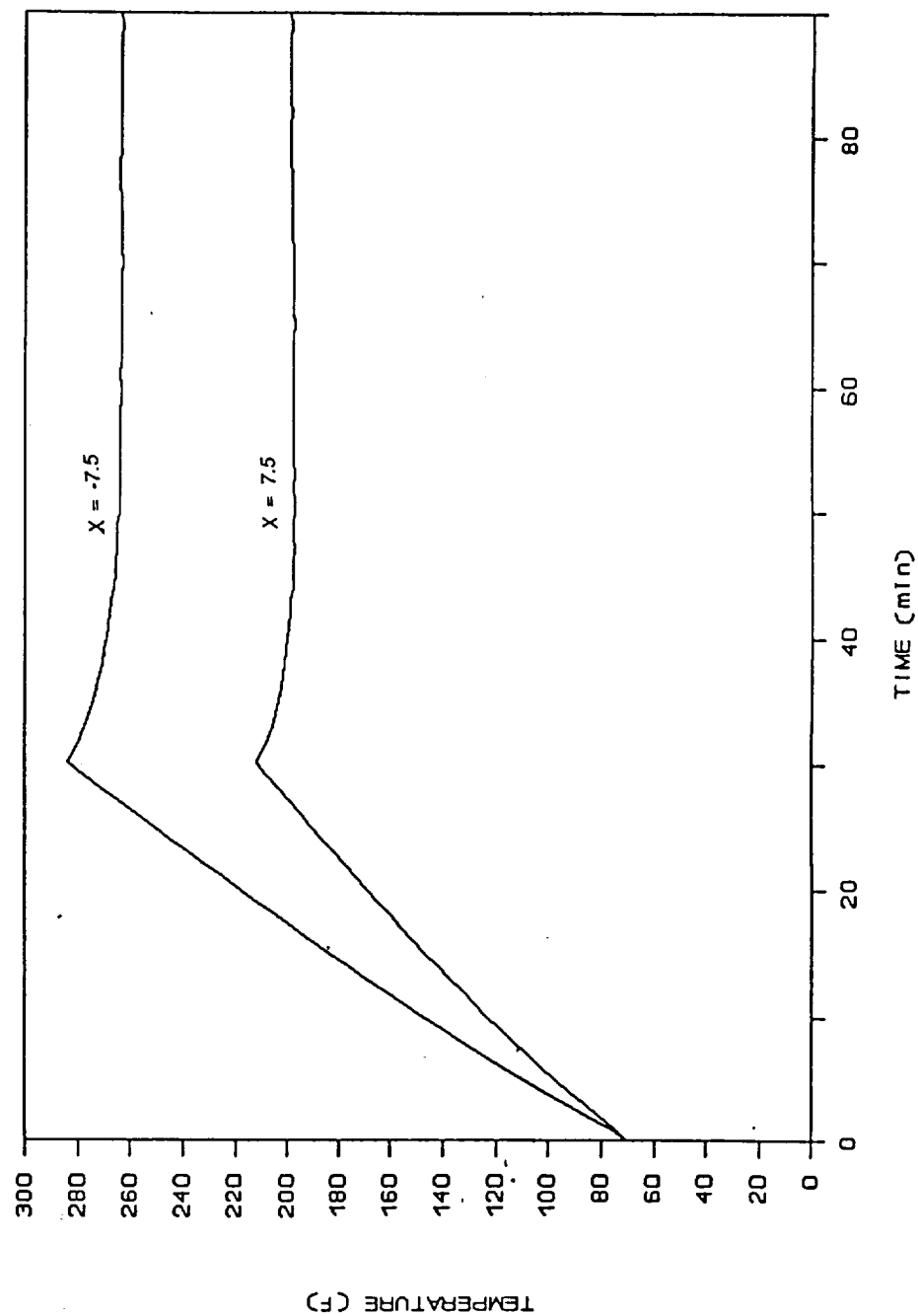


# EXPERIMENTAL TEMPERATURES FOR TEST PANEL TEMPERATURES TAKEN ALONG Y AXIS VARYING WITH TIME



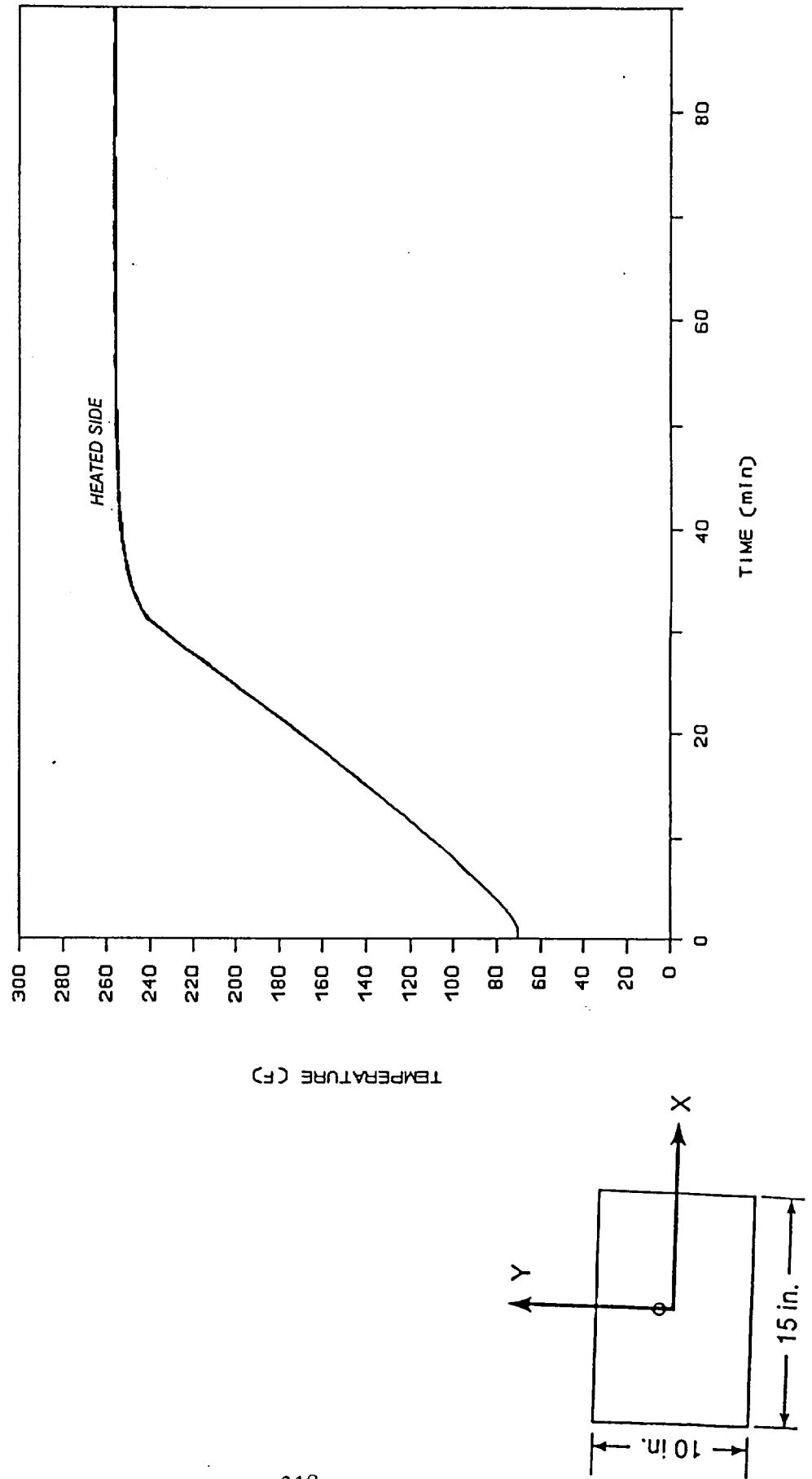
# EXPERIMENTAL TEMPERATURES FOR TEST PANEL

TEMPERATURES TAKEN AT  $X = \pm 7.5$ ,  $Y = 0$



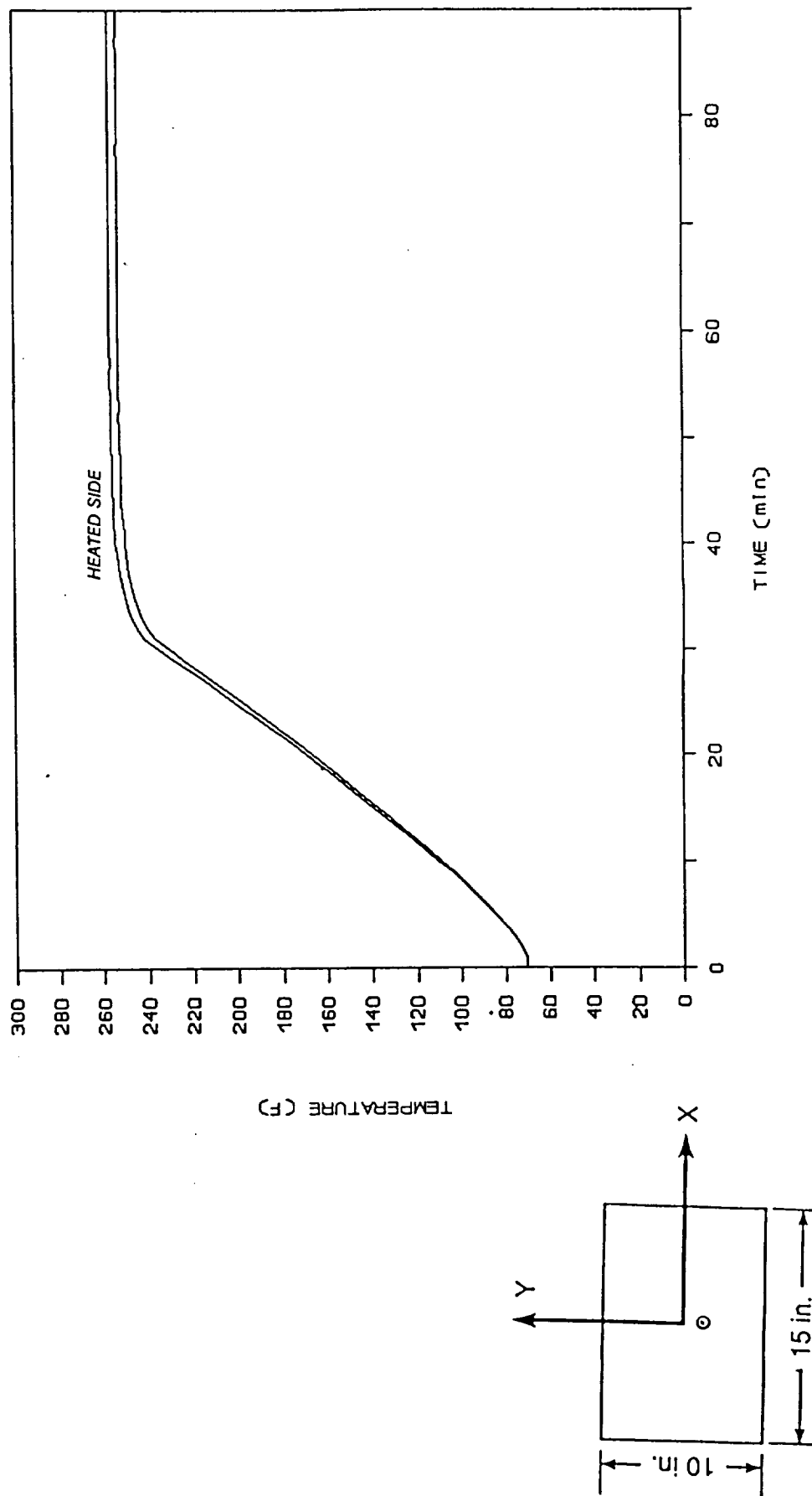
EXPERIMENTAL TEMPERATURES FOR TEST PANEL

THROUGH THE THICKNESS TEMPERATURE VARIATION ( $X = 0, Y = 1$ )



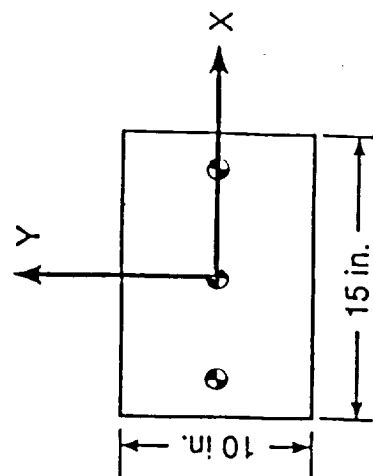
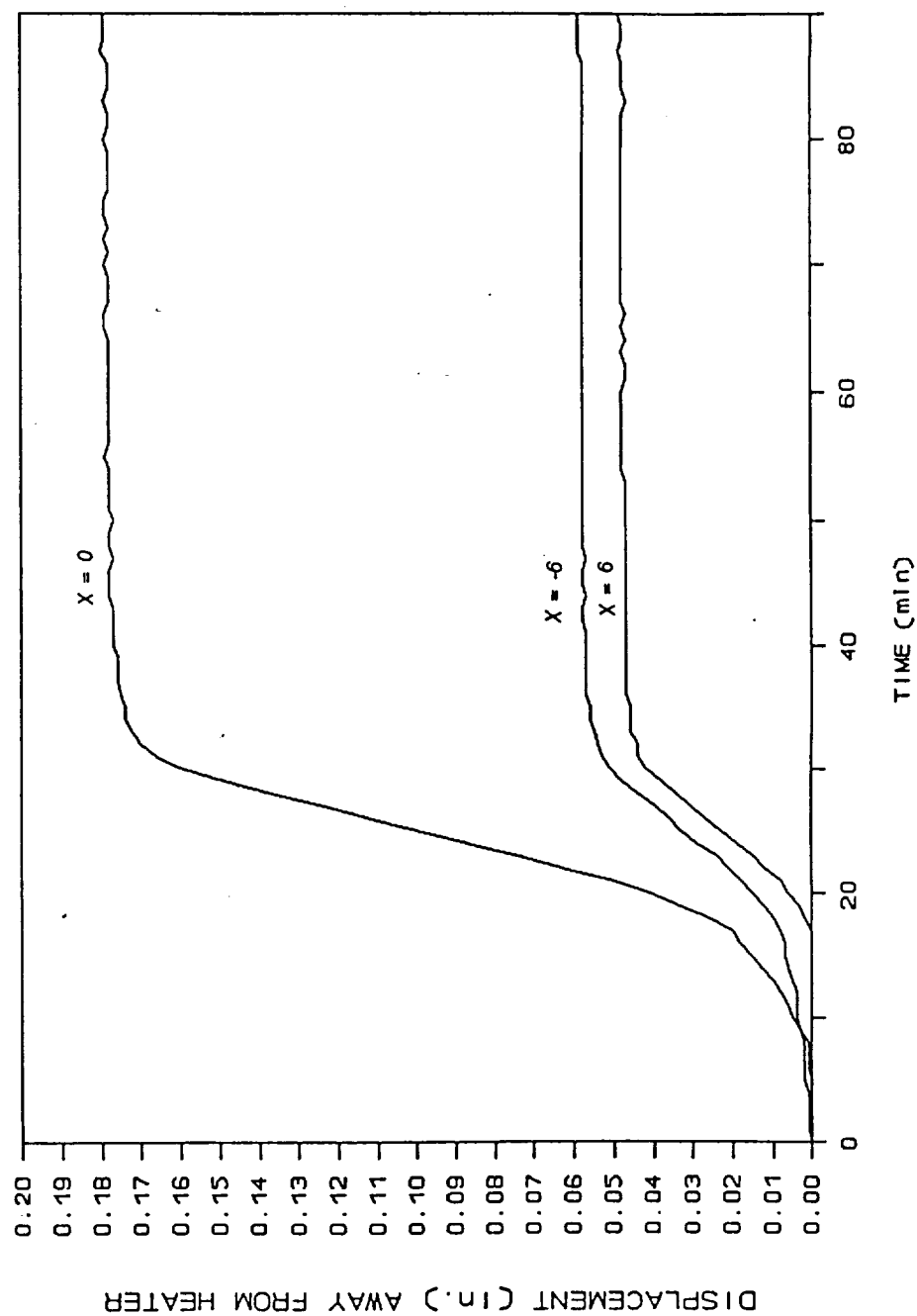
# EXPERIMENTAL TEMPERATURES FOR TEST PANEL

THROUGH THE THICKNESS TEMPERATURE VARIATION ( $X = 0$ ,  $Y = -1$ )



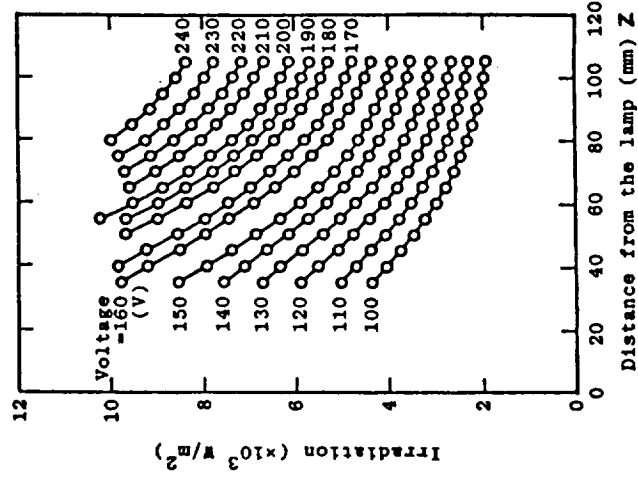
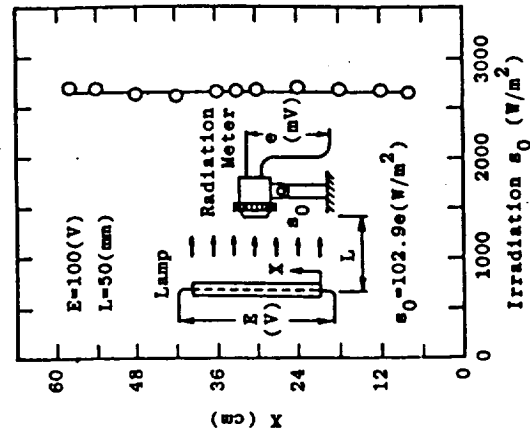
# EXPERIMENTAL DISPLACEMENTS FOR TEST PANEL

## DISPLACEMENT OF THE PANEL ALONG X AXIS



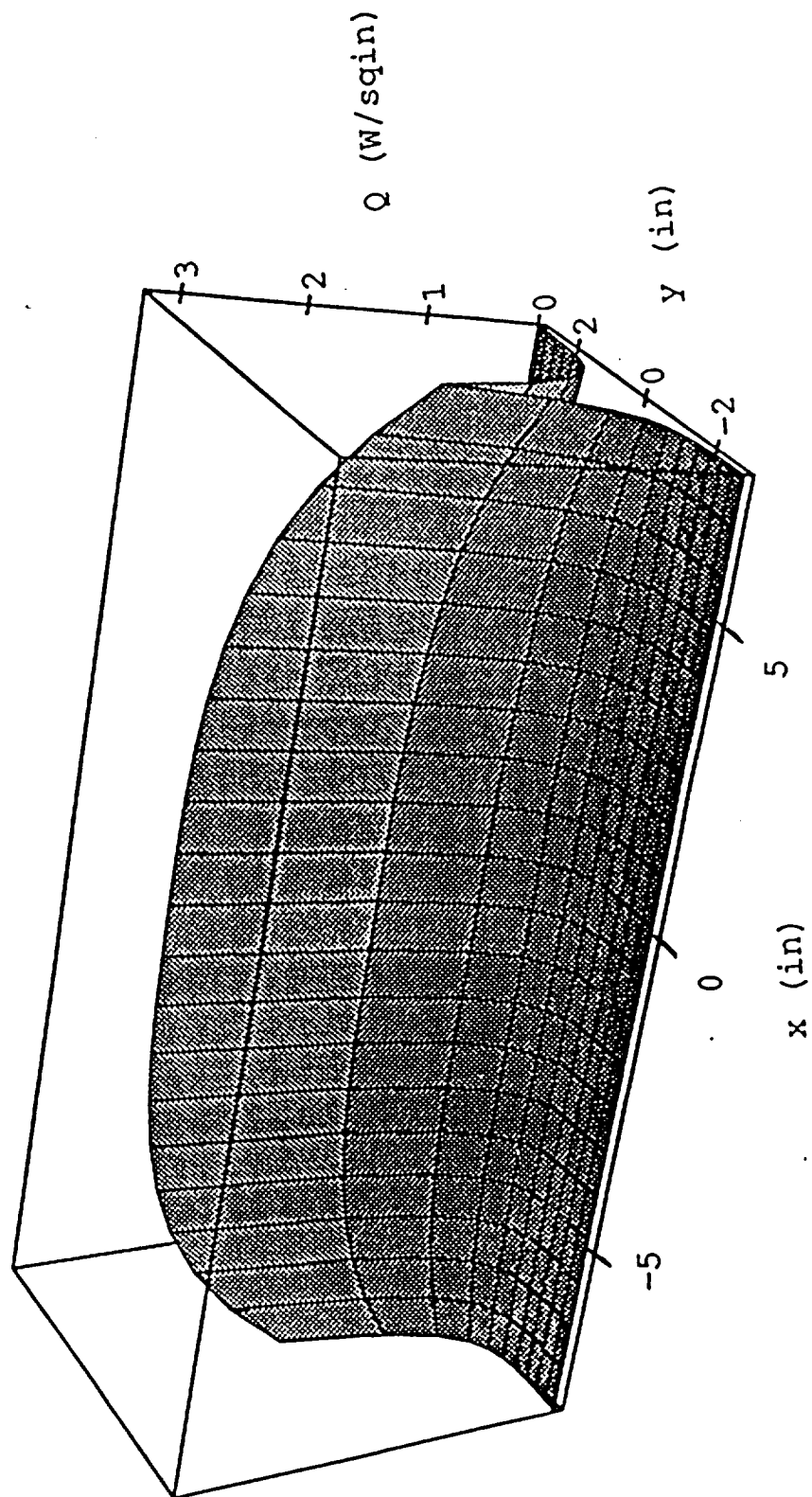
## HEAT LAMP INCIDENT FLUX VARIATIONS

- PRELIMINARY TESTS INDICATE SIGNIFICANT FLUX VARIATION IN X-Y FOCAL PLANE
- SUMI (REF. 6) FOUND MAJOR VARIATION OF FLUX WITH DISTANCE Z FROM LAMP



- DEPENDENCE OF FLUX ON Z COULD COUPLE THERMAL AND STRUCTURAL RESPONSE
- AUTOMATED "X-Y-Z" FLUX MEASUREMENT FIXTURE UNDER DEVELOPMENT

LINE HEATER MEASURED  
INCIDENT HEAT FLUX AT FOCAL PLANE





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## *FUTURE RESEARCH PLANS*

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- *LAMP CHARACTERIZATION TESTS*
- *ACQUIRE STRAIN GAGE DATA ACQUISITION SYSTEM*
- *CONTINUED TESTS OF HASTELLOY-X PANELS*
- *TEST PANEL WITH STRAIN GAGES*
- *BEGIN CORRELATION WITH ANALYSIS*

## CONCLUDING REMARKS

Recent progress of a research program focused on understanding the thermoviscoplastic behavior of structural panels is described. The program has three tasks: (1) finite element simulations of nonlinear material and geometric behavior, (2) experimental determination of parameters for the Bodner-Partom constitutive models of panel materials, and (3) thermal-structural tests of panels subjected to localized heating.

Plane stress finite element computations are providing insight into panel behavior under different experimental conditions and have shown the importance of thermal loading rates. Finite element analysis of nonlinear panel bending is under development. This capability will permit the simulation of the panel tests and direct correlation of predicted displacements and strains with measured values.

A research task focused on the experimental determination of the constitutive model parameters was recently initiated. This task will provide data for the panel materials for the range of temperatures and strain rates to be used in the thermal-structural test program. Initial tests will be conducted for the available Hastelloy X material; later tests will characterize the 8009 aluminum alloy as material becomes available.

Thermal-structural testing has progressed with the design and fabrication of a panel test fixture. The fixture supports the quartz lamp line heater, the coolant system and panel insulation. It also provides point supports for a panel and supports for LVDTs to measure panel displacements. Preliminary tests have measured Hastelloy-X panel temperature and displacement histories. Unexpected variations of panel temperatures appear to be related to nonuniform incident panel heat fluxes. An experimental program to investigate lamp heat flux variations was recently initiated.

Future plans include continued development of each of the research tasks. Within the next year correlations of simulated thermoviscoplastic panel behavior with experimental data will be initiated.

## REFERENCES

1. Heldenfels, Richard R. and Roberts, William M.: "Experimental and Theoretical Determination of Thermal Stresses in a Flat Plate," NACA TN 2769, 1952.
2. Gossard, Myron L., Seide, Paul and Roberts, William M.: "Thermal Buckling of Plates," NACA TN 2771, 1952.
3. Thornton, Earl A., Oden, J. Tinsley, Tworzydlo, W. Woytek and Youn, Sung-Kie: "Thermo-Viscoplastic Analysis of Hypersonic Structures Subjected to Severe Aerodynamic Heating," Journal of Aircraft, Vol. 27, No. 9, Sept. 1990, pp. 826-835.
4. Pandey, A. K., Dechaumphai, P. and Thornton, E. A.: "Finite Element Thermo-Viscoplastic Analysis of Aerospace Structures," Proceedings of the First Thermal Structures Conference, University of Virginia, Nov. 13-15, 1990, pp. 169-189.
5. Thornton, Earl A. and Kolenski, J. D.: "Viscoplastic Response of Structures with Intense Local Heating," AIAA Paper No. 91-1149, AIAA/ASME/ASCE/AHS/ASC 32nd Structures, Structural Dynamics and Materials Conference, April 8-9, 1991, Baltimore, MD.
6. Sumi, S.: "Thermally Induced Bending Vibration of Thin Walled Boom Caused by Radiant Heating," Trans. Japan Society of Mechanical Engineers, Vol. 56, pp. 300-307, 1990.